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Energy Markets
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Improving the Coordination between Electricity and Gas Systems: A Distributed Market -Clearing Approach

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Open-Minded

Motivation

1

Status quo & towards a novel market clearing framework

2

Case study: German electricity & natural gas systems

3

Case study: Results

4

Conclusion & outlook

5

1

2

3

4

5

General challenges



Decarbonization

- High shares of renewables require infrastructure expansion + flexibility



Decentralization

- Spatio-temporal decoupling of generation and demand



Digitalization

- Extended possibilities of interconnection and participation, e.g., of „prosumers“

Existing coordination approaches



Central coordination: Requires some kind of third-party operator (e.g., an ISO) + disclosure of commercial sensitive information ^[3]



Decentralized coordination: Either local third-party operators ^[4] (+ information disclosure) or peer-to-peer trading, lacking scalability ^[5] + too complex ^[6]

Specific challenges



Compliance with EU regulation ^[1]

- Confidentiality of sensitive comm. information
- Understandable transparent market rules



Risks and uncertainty of cross-sector operation

- Trading energy (electricity and gas) on multiple asynchronous markets leads to inefficiencies ^[2]



Flexibility market-integration

- Coordination of intertemporal constraints required to incentivize congestion relief

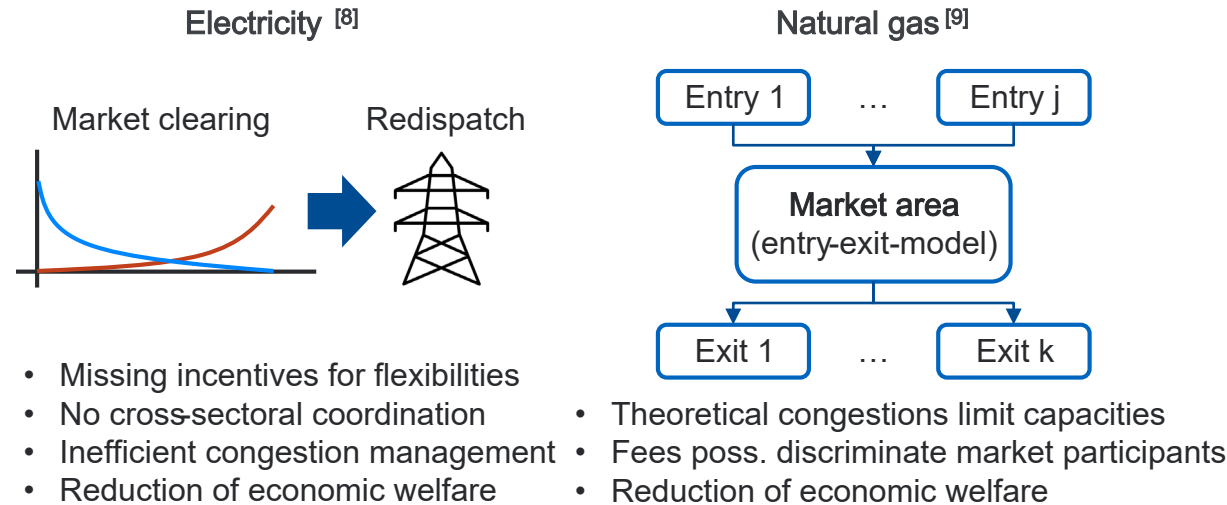
Requirements for a coordination mechanism

Independence of units: Preserve confidentiality ^[1]

Limited exchange of information:
Limited knowledge of other networks & units ^[7]

Reliability & scalability: Large-scale applications

Status quo: Market & network operation (in Germany)



Locational marginal prices (LMPs) & crosssector coordination

Natural gas

- Only actual congestions limit technical capacities
- LMPs adequately allocate network usage and congestions

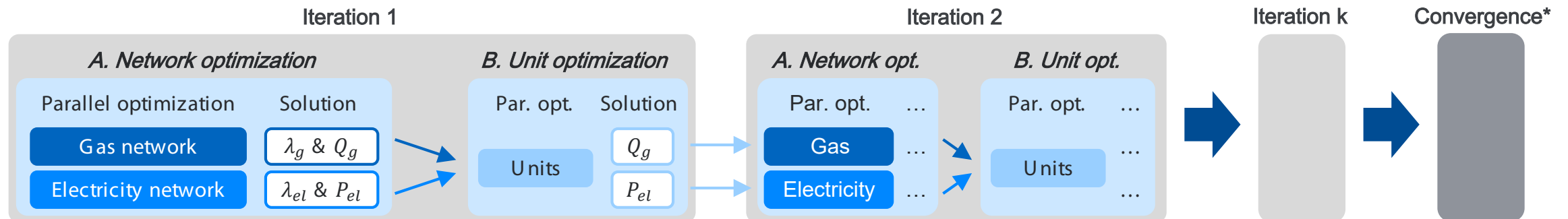
Electricity

- Local incentives for flexibilities to avoid congestions
- Joint market clearing and congestion mgmt.

Cross-sectoral

- Empowering usage of cross-sectoral flexibility
- Reducing complexity for cross-sectoral units by harmonizing asynchronous market clearings
- Leveraging economic welfare

Proposed architecture: Distributed iterative multi-period market clearing



Casestudy: German electricity & natural gas systems(24-h)

1 2 3 4 5

- Electricity network data^[11]
 - LKD-EU – Reference data (2017)

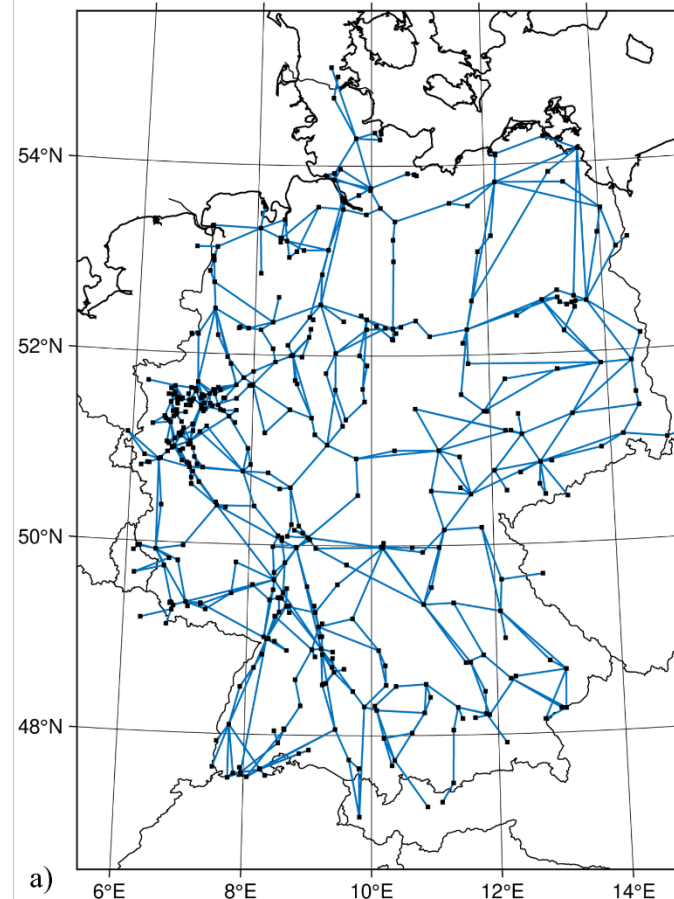
Elements	No.
Nodes	450
Transmission lines	724

- Gas network data^[12]
 - SciGRID_gas data

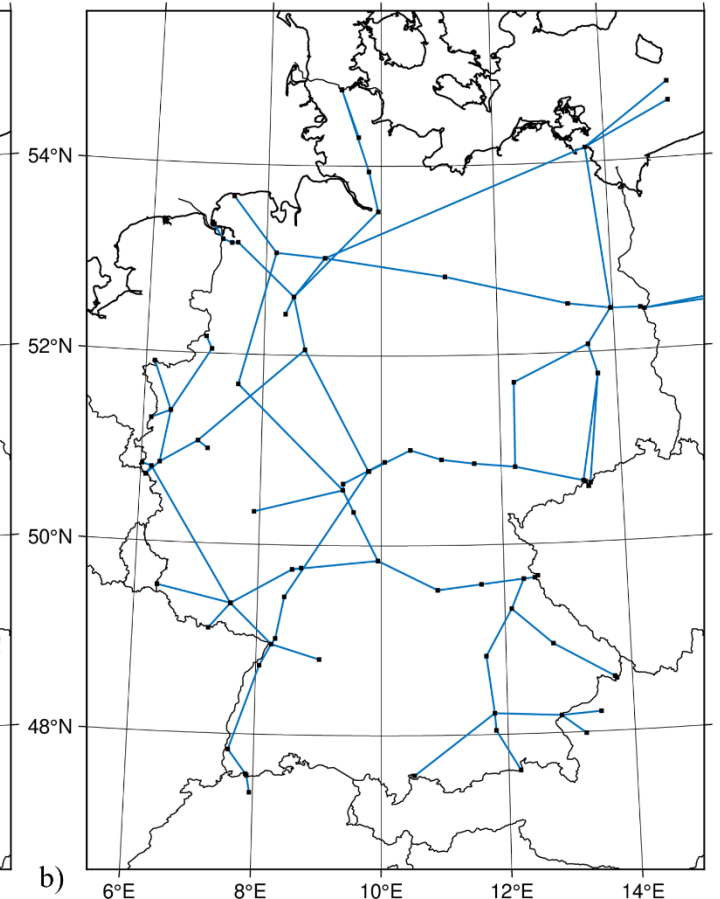
Elements	No.
Compressor stations	32
Nodes	202
Pipeline segments	123
Supply nodes	33

- Time-series data (demand & renewables)
 - Typical winter day 24 h period
 - Reference year: 2017

Electricity network



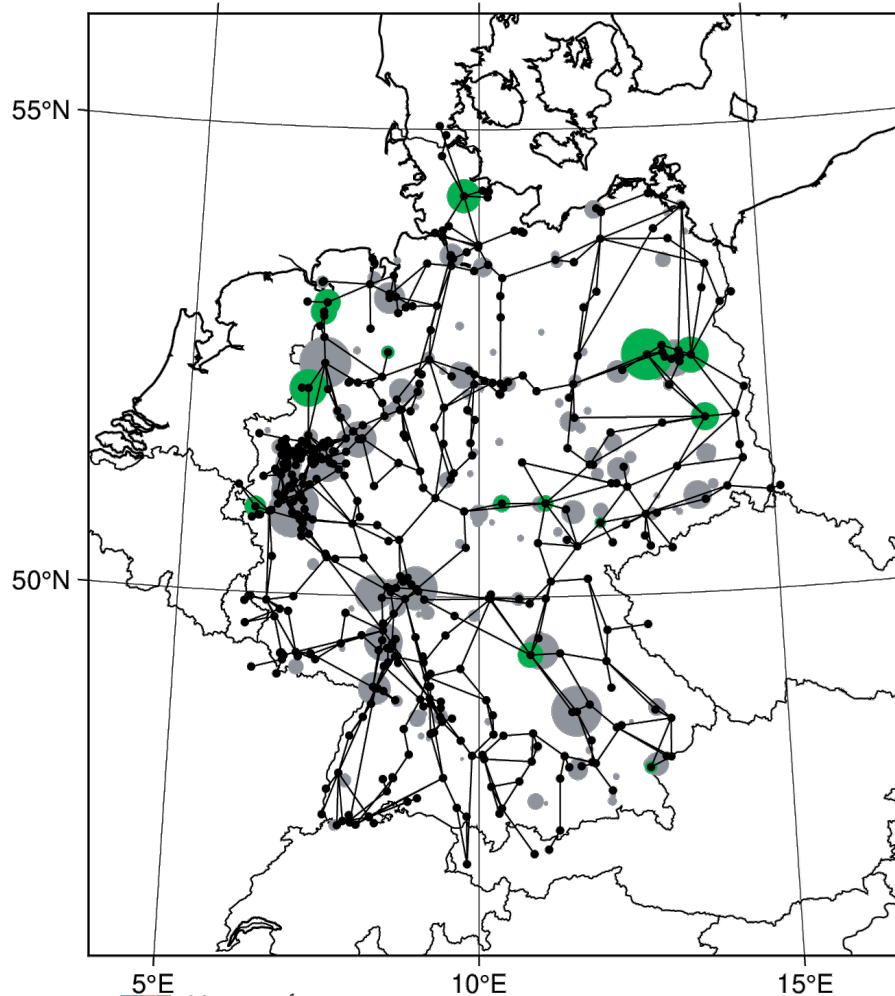
Natural gas network



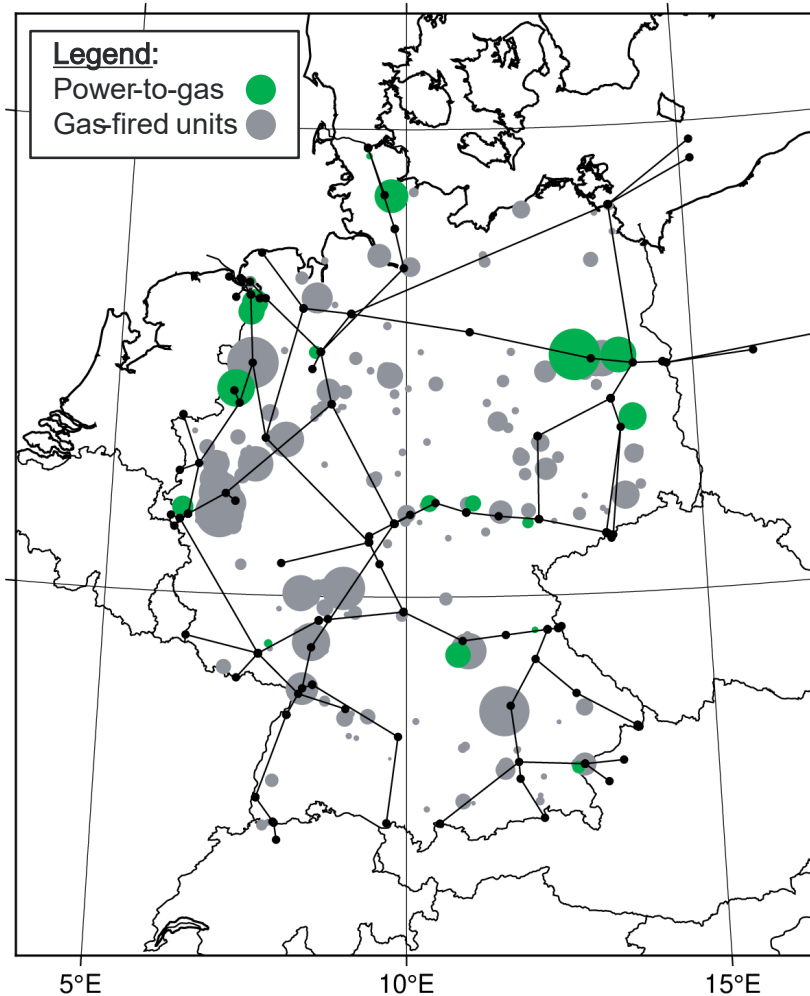
Casestudy: Cross-sectoral units & capacities

1 2 3 4 5

Electricity network



Natural gas network

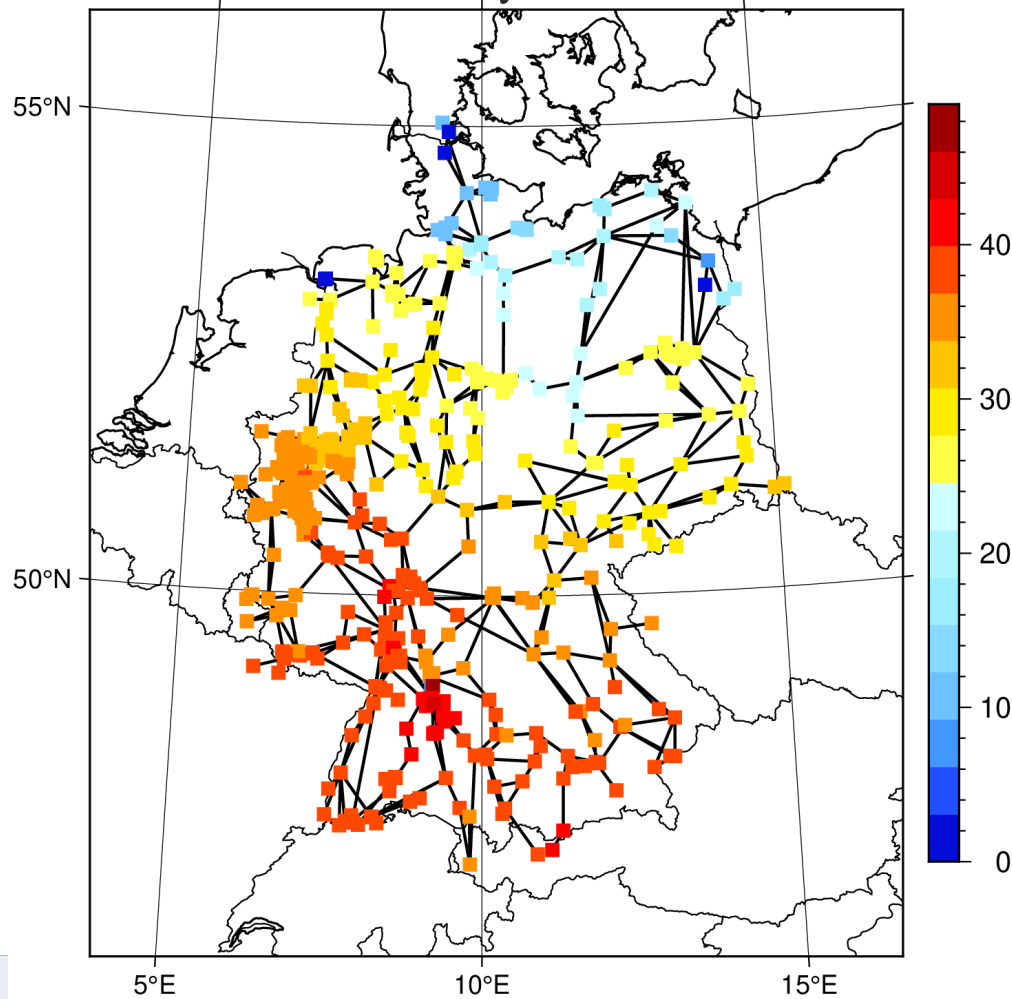


Technology	Capacity (in GW)	No.
Power-to-gas	5.06	19
Gas-fired units	23.62	271
Solar	26.23	315
Wind	35.11	269
Conventionals	79.30	436

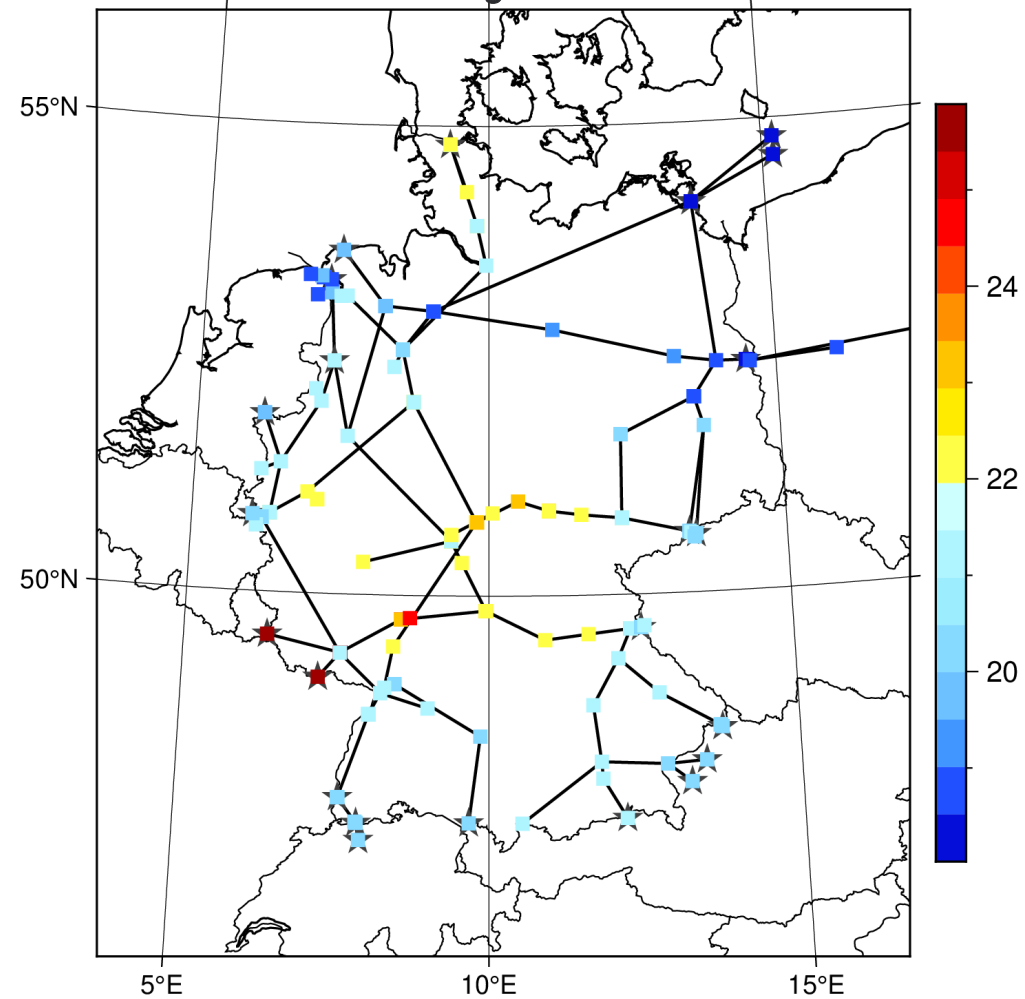
Case study: Economic results- LMPs (in EUR/MWh)

1 2 3 4 5

Electricity network



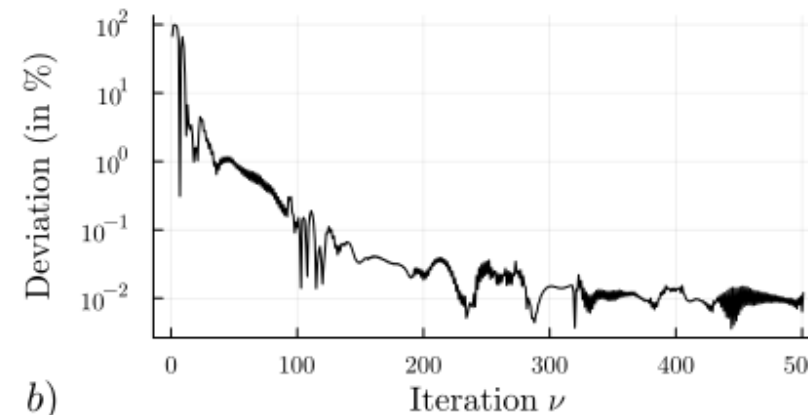
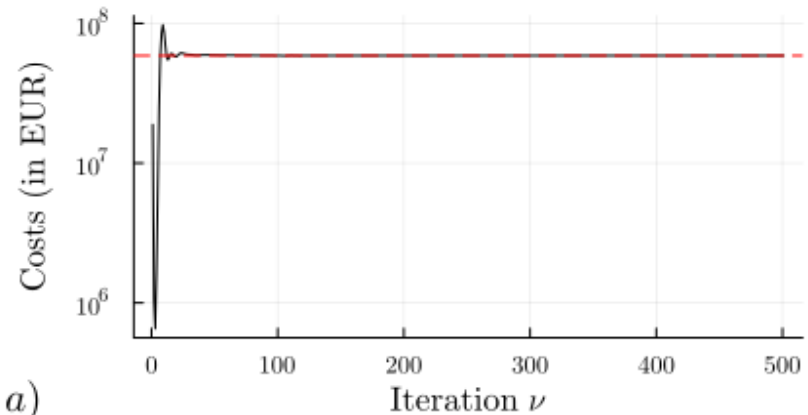
Natural gas network



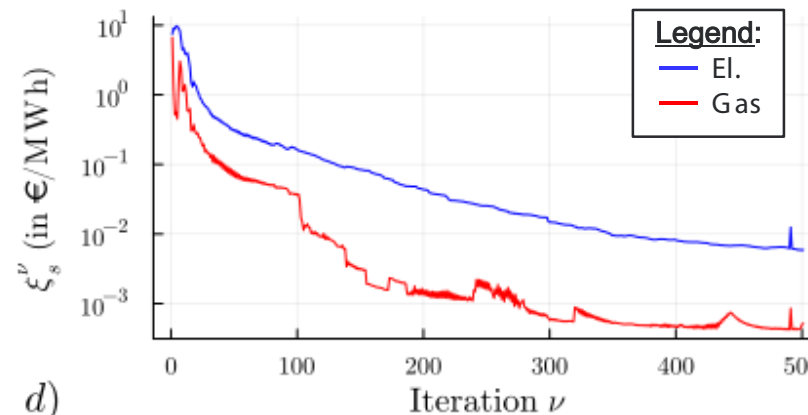
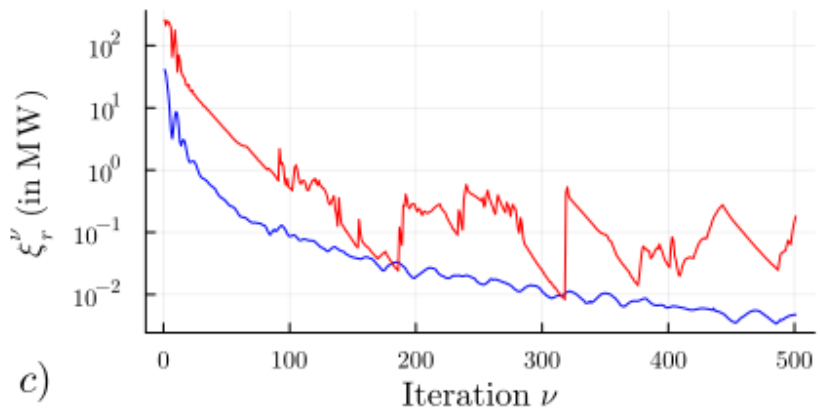
Case study: Results- Distributed market clearing (1/2)

1 2 3 4 5

Total system costs- Absolute value & deviation



NRMSE- ξ_r^ν : network vs. unit results & ξ_s^ν : successive price updates



- Objective function
 - Deviation drops below 0.1 % after 110 iterations
- NRMSE (for each unit and hour) after 140 iterations:
 - Deviation between networks' and units' results falls below:
 - EL: 0.1 MW (for each hour)
 - Gas: 1 MW (for each hour)
 - Change of price updates between two iterations
 - EL: 0.1 €/MWh
 - Gas: 0.01 €/MWh
- Preliminary conclusion
 - Changes on a holistic level appear to be reasonably small
 - indicating convergence

Dispatch (in GWh) for 24-h after $\nu = \{250, 500\}$ iterations

	Technology	Single operator	DMC		Difference	
			$\nu = 250$	$\nu = 500$	$\nu = 250$	$\nu = 500$
Electricity	Conventionals	637.54	637.27	637.89	-0.27	0.35
	Wind	617.77	617.12	617.25	-0.65	-0.52
	Solar	7.26	7.33	7.42	0.07	0.16
	Gas-fired	96.95	98.22	97.06	1.27	0.11
	Power-to-gas	19.6	19.87	19.68	0.27	0.08
	Demand	1,262.76	1,262.87	1,262.75	0.11	-0.01
	Wind curt.	35.12	35.76	35.63	0.64	0.51
	Solar curt.	0.32	0.26	0.16	-0.06	-0.16
	Demand shed.	0	-0.11	0.01	-0.11	0.01
	Total supply	1,359.52	1,359.93	1,359.62	0.41	0.1
Total demand	1,282.36	1,282.74	1,282.43	0.38	0.07	
Trans. losses	77.16	77.19	77.19	0.03	0.03	
Natural gas	Import	6,529.11	6,531.36	6,529.28	2.25	0.17
	Power-to-gas	12.77	12.95	12.82	0.18	0.05
	Gas-fired	169.36	171.6	169.51	2.24	0.15
	Export	2,036.71	2,036.71	2,036.72	0	0.01
	Res. demand	2,852.13	2,852.13	2,852.16	0	0.03
	Ind. demand	1,076.71	1,076.71	1,076.74	0	0.03
	Export shed.	0	0	0	0	0
	Res. shed.	0	0	0	0	0
	Ind. shed.	0	0	0	0	0
	Total supply	589.36	589.58	589.38	0.22	0.02
Total demand	552.7	552.9	552.71	0.2	0.01	
Trans. losses	36.66	36.68	36.66	0.02	0	

- Overall observations for DMC
 - Deviations per technology are relatively small
 - Total supply, demand and losses are met better
- How imperfect is the DMC? Largest deviations
 - 250 iterations: 2.25 GWh (day) ~ 93.75 MWh (hour)
 - 500 iterations: -0.52 GWh (day) ~ 21.67 MWh (hour)
- Insights into DMC imperfections:
 - Units with (almost) identical costs are affected most
 - Renewables, conventionals, gas imports and exports
 - Sector coupling units take longer to converge
 - Two prices need to converge properly

- Distributed market clearing (DMC)
 - Could serve as a basis for cross-sector coordination, preserving independence of units
 - Suitable for large-scale applications with limited information exchange
- Implementational aspects
 - Today, low latency **algorithmic traders** react to capital markets in under 1 ms
 - DMC with approx. 10^3 iterations could be achieved **within a couple of seconds**
 - Crucial factors:
 - Processing time of network and unit optimization
 - Physical distance between units and network operators
 - Handling of communication and algorithmic errors
- Handling of non-convexities
 - Despite the availability of proper & tight convex relaxations: More accurate models for unit commitment and gas network operation require mixed-integer models
 - Non-convexities lead to distortions and question the interpretability of prices
 - Revenue adequacy and cost recovery not guaranteed
- Extension of framework
 - Integration of balancing markets and ancillary services procurement
 - Integration of multiple network operators and distribution networks
 - Investigation of market power within a DMC

Thank you for your attention!

Aiko Schinke-Nendza (M.Sc.)

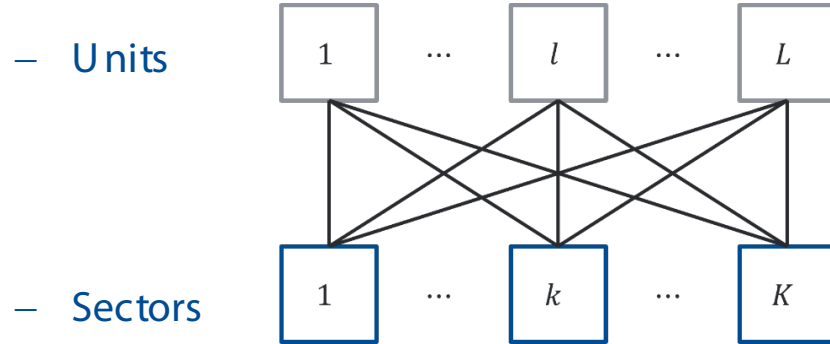
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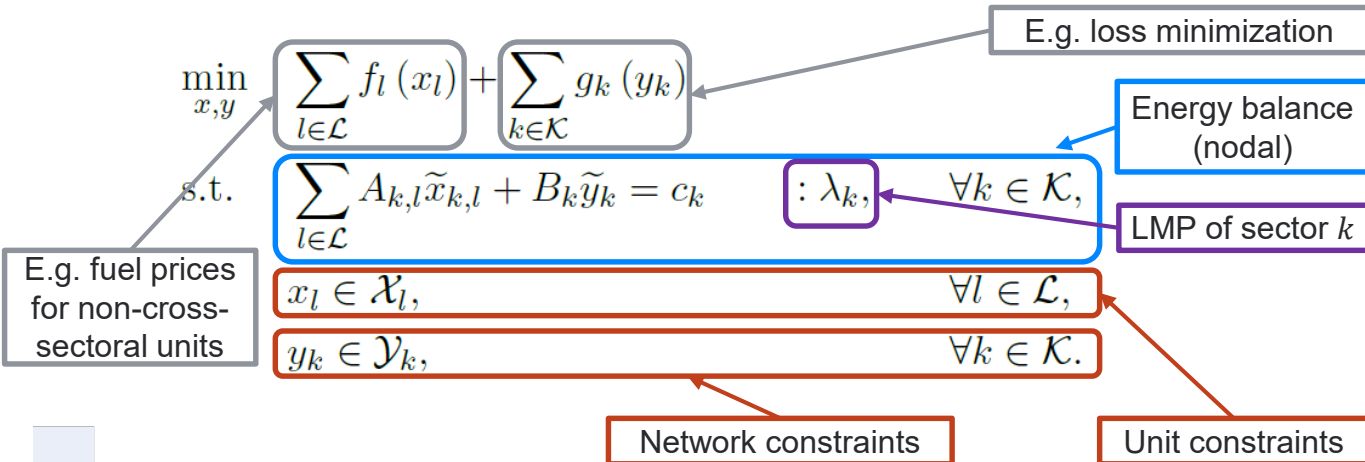


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- Abstract structure



- Convex multi-period problem: An omniscient single-operator



- Distributed market clearing* (Iteration ν)

- Unit subproblem

$$\min_{x_l} f_l(x_l) + \sum_{k \in \mathcal{K}} \left[-(\lambda_{k,l}^{\nu-1})^\top \tilde{x}_{k,l} + \frac{\rho_k}{2} \|\psi_{k,l}^{\nu-1} - \tilde{x}_{k,l}\|_2^2 \right]$$

s.t. $x_l \in \mathcal{X}_l,$

- Sectoral network subproblem

$$\min_{y_k} g_k(y_k) + \sum_{l \in \mathcal{L}} \left[(\lambda_{k,l}^{\nu-1})^\top \psi_{k,l} + \frac{\rho_k}{2} \|\psi_{k,l} - \tilde{x}_{k,l}^{\nu-1}\|_2^2 \right]$$

s.t. $y_k \in \mathcal{Y}_k,$

- Price updates (with constants φ_k^ν and ρ_k^ν)

$$\lambda_{k,l}^{\nu+1} = \lambda_{k,l}^\nu + \varphi_k^\nu \rho_k^\nu (\psi_{k,l}^\nu - \tilde{x}_{k,l}^\nu),$$

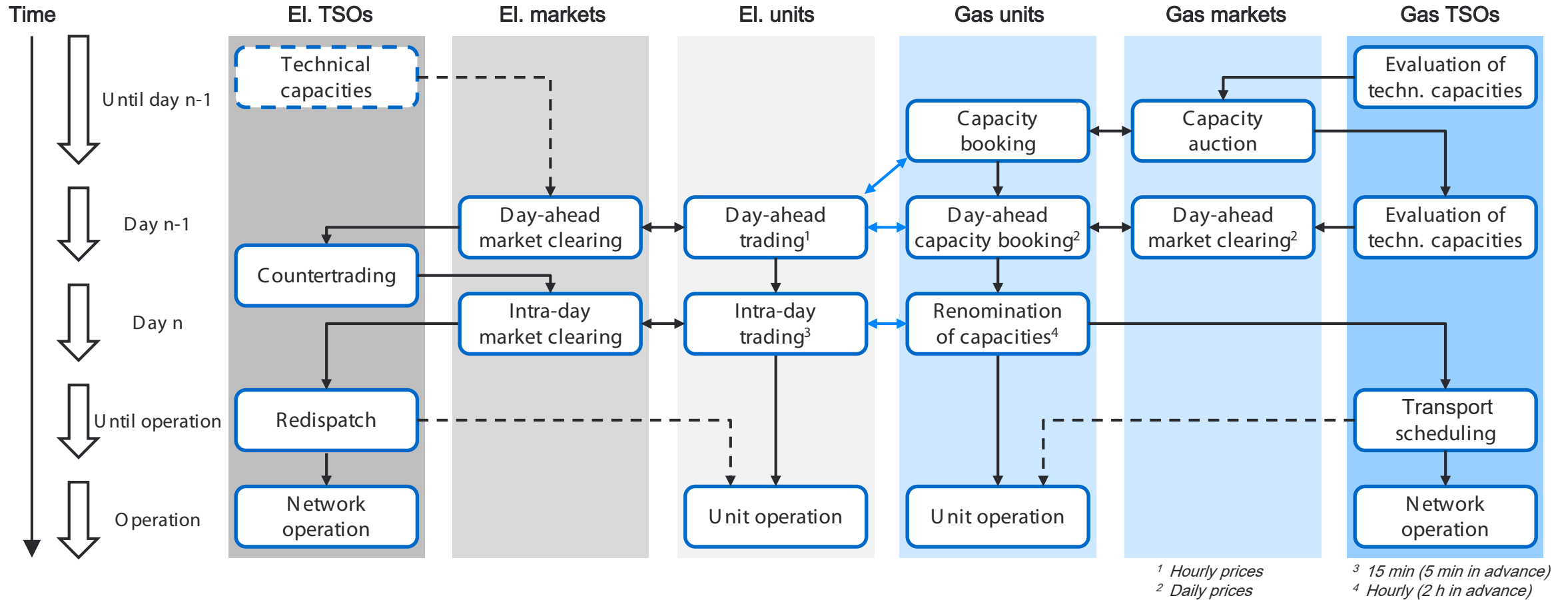
- Reformulating balances as part of networks

$$\sum_{l \in \mathcal{L}} A_{k,l} \psi_{k,l} + B_k \tilde{y}_k = c_k, \quad : \lambda_{k,n}, \quad \forall k \in \mathcal{K},$$

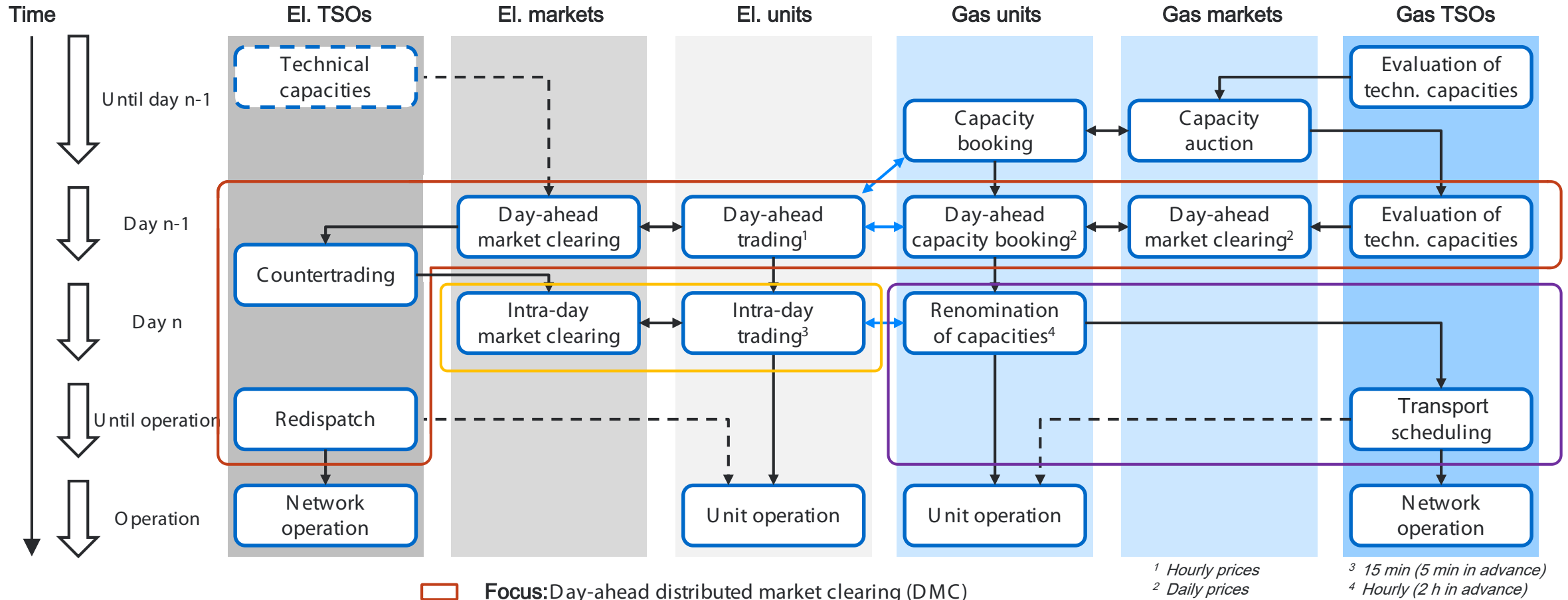
$$\psi_{k,l} = \tilde{x}_{k,l}, \quad \forall l \in \mathcal{L}, \forall k \in \mathcal{K}.$$

* Using decomposition techniques, here, alternating direction method of multipliers (ADMM), cf. [10]

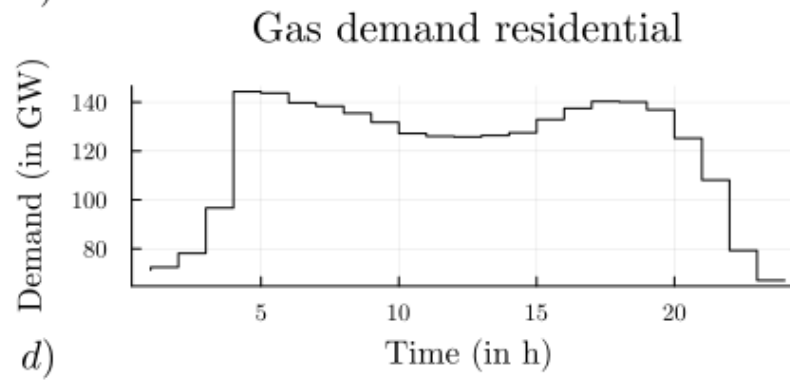
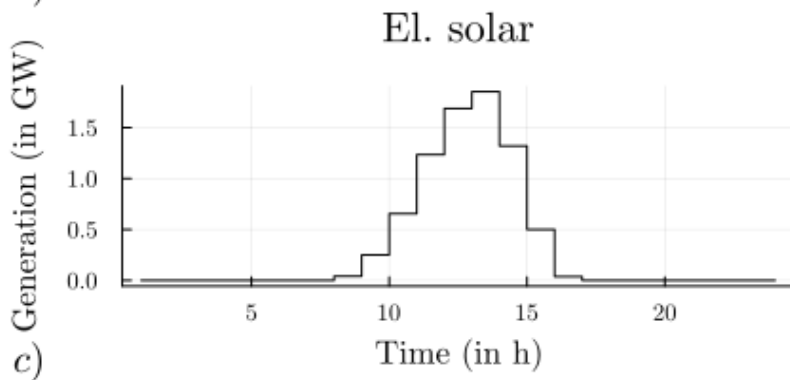
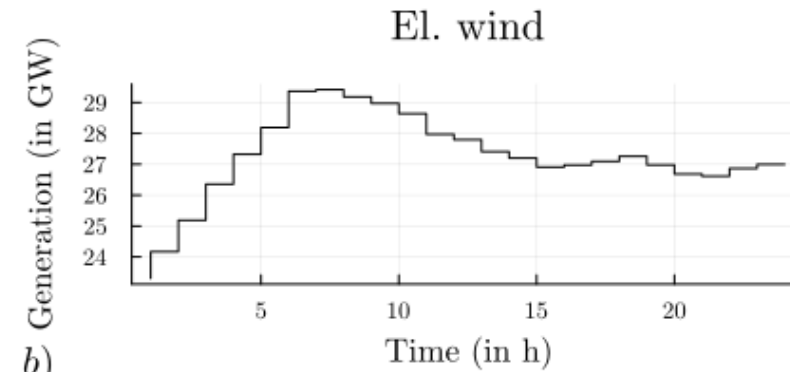
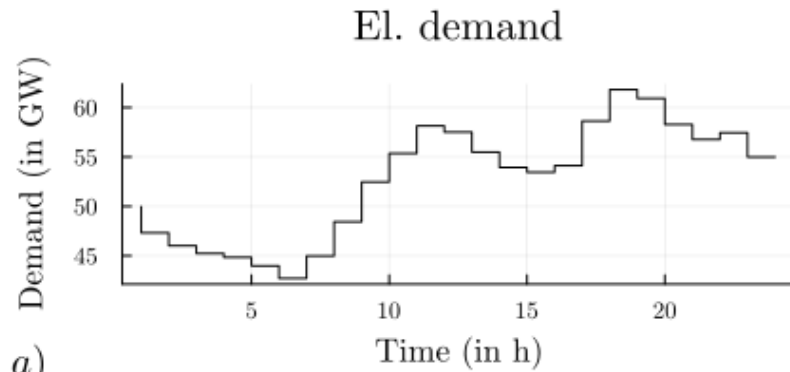
Backup: Existing market design in Germany



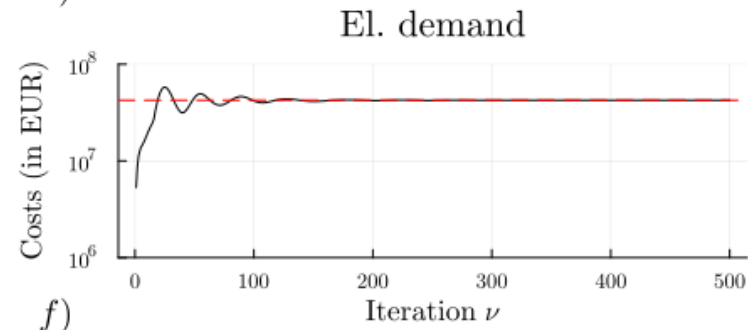
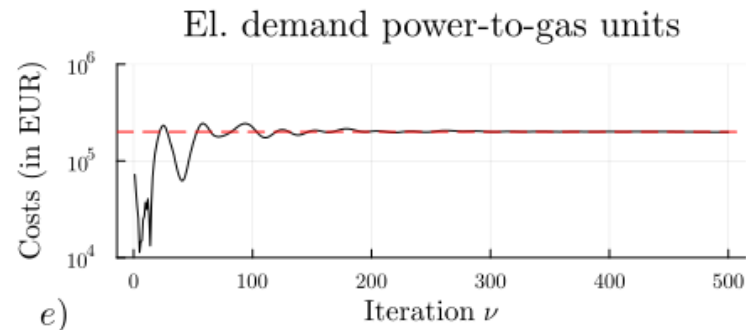
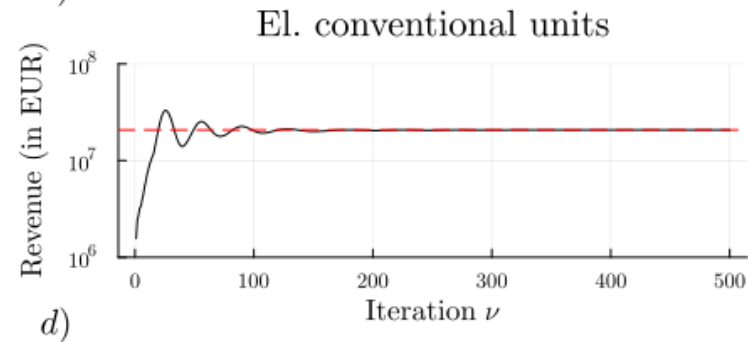
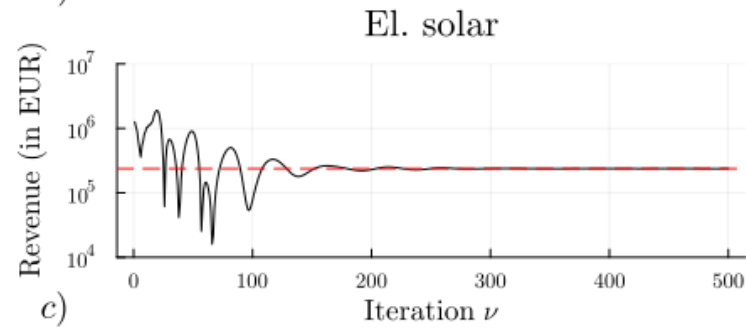
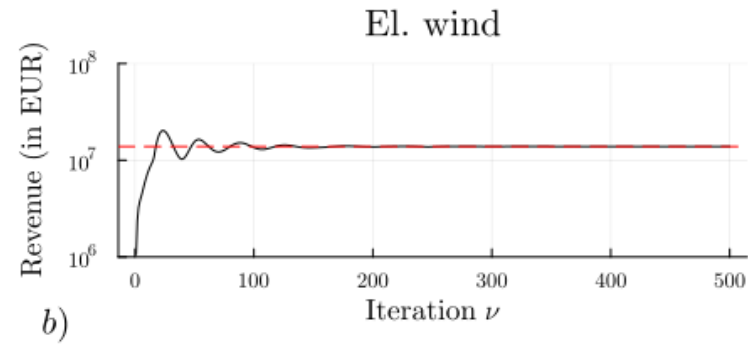
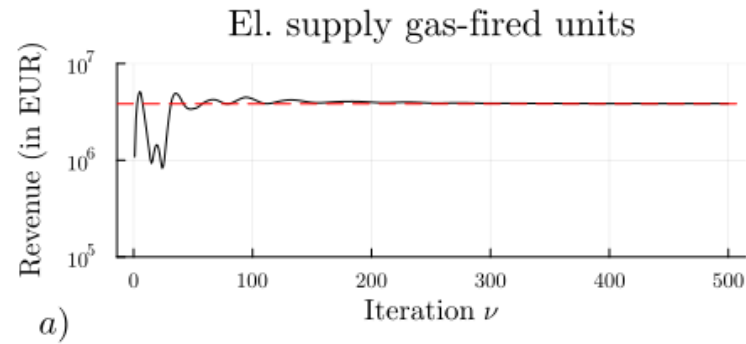
Backup: Existing market design in Germany



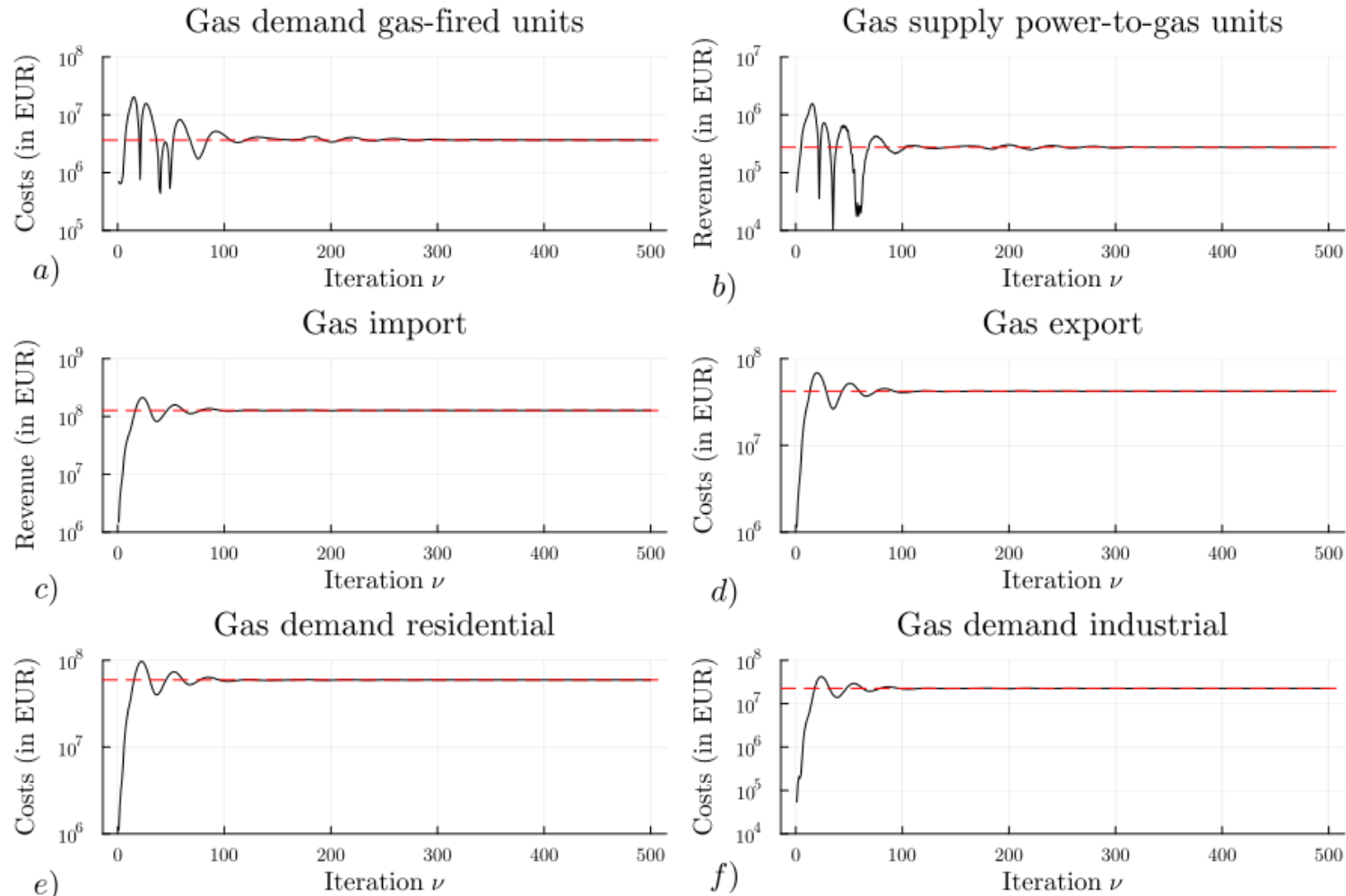
Backup: Electricity and gas time-series data



Backup: Convergence on a technology level- EL



Backup: Convergence on a technology level- Gas



$$\min_{\Xi_t^{gas}, \Theta_t^{gas}} \sum_{t \in \mathbb{T}, m \in \mathbb{M}} \left[\sum_{s \in \mathbb{S}(m)} c_s^{gas,S} Q_{s,t}^S + c_m^{gas,VOLL} (Q_{m,t}^{D+} - Q_{m,t}^D) + c_m^{gas,Ex} (Q_{m,t}^{D,Ex+} - Q_{m,t}^{D,Ex}) \right] \Delta t, \quad (20a)$$

$$\text{s.t.} \quad Q_{m,t}^{N,S} + Q_{m,t}^F + Q_{m,t}^C + Q_{m,t}^{N,S,PtG} = Q_{m,t}^D + Q_{m,t}^{N,D,GFU} + Q_{m,t}^{D,Ex}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20b)$$

$$Q_{m,t}^{N,S} = \sum_{s \in \mathbb{S}(m)} Q_{s,t}^S, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20c)$$

$$Q_{m,t}^{N,S,PtG} = \sum_{k \in \mathbb{K}_{gas}^{PtG}(m)} Q_{k,t}^{S,PtG}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20d)$$

$$Q_{m,t}^{N,D,GFU} = \sum_{k \in \mathbb{K}_{gas}^{GFU}(m)} Q_{k,t}^{D,GFU}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20e)$$

$$p_m^{\min} \leq p_{m,t} \leq p_m^{\max}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20f)$$

$$0 \leq Q_{s,t}^S \leq Q_{s,t}^{S+}, \quad \forall s \in \mathbb{S}, t \in \mathbb{T}, \quad (20g)$$

$$0 \leq Q_{m,t}^D \leq Q_{m,t}^{D+}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20h)$$

$$0 \leq Q_{m,t}^{D,Ex} \leq Q_{m,t}^{D,Ex+}, \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20i)$$

$$Q_{m,t}^C = \sum_{n \in \mathbb{C}^{in}(m)} (Q_{m,n,t}^{C,In} - Q_{m,n,t}^{C,Out}) + \sum_{n \in \mathbb{C}^{out}(m)} (Q_{n,m,t}^{C,In} - Q_{n,m,t}^{C,Out}), \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20j)$$

$$Q_{n,m,t}^{C,Out} = Q_{m,n,t}^{C,In}, \quad \forall m, n \in \mathbb{C}, t \in \mathbb{T}, \quad (20k)$$

$$Q_{m,n,t}^{C,Out} = Q_{n,m,t}^{C,In} + Q_{m,n,t}^{C,Loss}, \quad \forall m, n \in \mathbb{C}, t \in \mathbb{T}, \quad (20l)$$

$$\alpha_m^{C,\min} p_{m,t} \leq p_{n,t} \leq \alpha_m^{C,\max} p_{m,t}, \quad \forall m, n \in \mathbb{C}, t \in \mathbb{T}, \quad (20m)$$

$$Q_{m,n,t}^{C,Out} \leq Q_{m,n}^{C,\max}, \quad \forall m, n \in \mathbb{C}, t \in \mathbb{T}, \quad (20n)$$

$$Q_{m,t}^F = \sum_{n \in \mathbb{P}^{in}(m)} (Q_{m,n,t}^{F,In} - Q_{m,n,t}^{F,Out}), \quad \forall m \in \mathbb{M}, t \in \mathbb{T}, \quad (20o)$$

$$\bar{Q}_{m,n,t}^F = (Q_{m,n,t}^{F,In} + Q_{m,n,t}^{F,Out}) / 2, \quad \forall m, n \in \mathbb{P}, t \in \mathbb{T}, \quad (20p)$$

$$\bar{Q}_{m,n,t}^F |\bar{Q}_{m,n,t}^F| = W_{m,n} (p_{m,t}^2 - p_{n,t}^2), \quad \forall m, n \in \mathbb{P}, t \in \mathbb{T}, \quad (20q)$$

$$\bar{V}_{m,n,t}^{LP} = K_{m,n}^{LP} (p_{m,t} + p_{n,t}) / 2, \quad \forall m, n \in \mathbb{P}, t \in \mathbb{T}, \quad (20r)$$

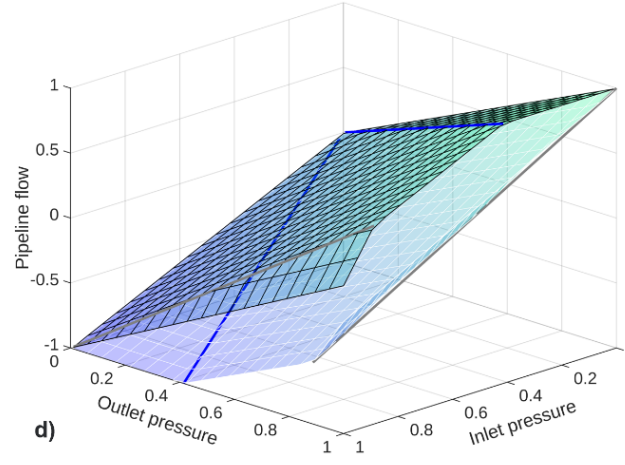
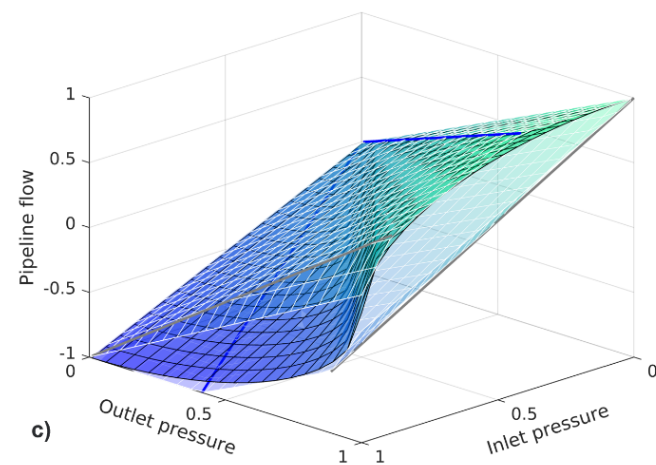
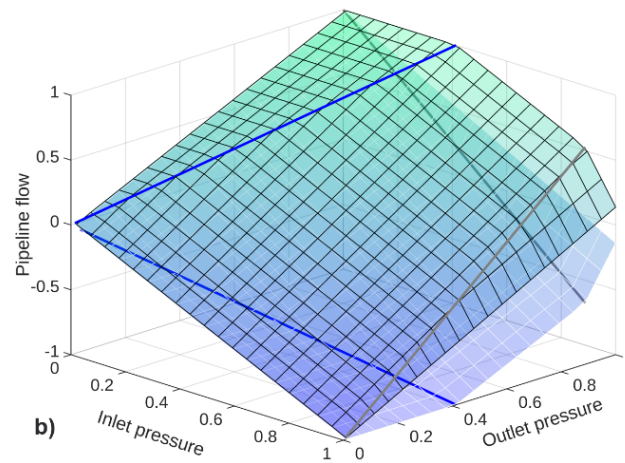
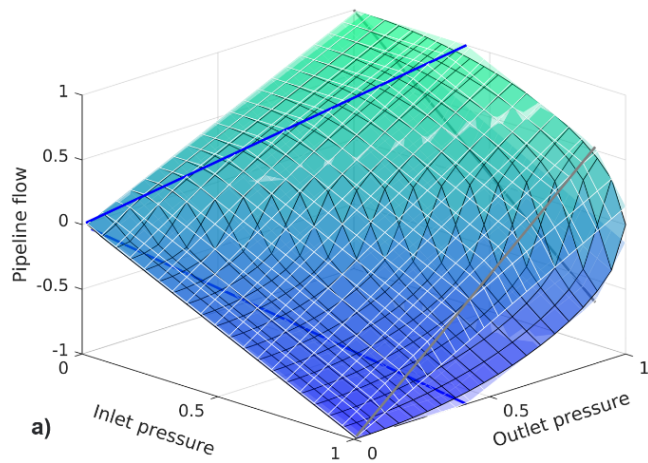
$$\Delta V_{m,n,t}^{LP} = (Q_{m,n,t}^{F,Out} - Q_{n,m,t}^{F,In}) \Delta t, \quad \forall m, n \in \mathbb{P}, t \in \mathbb{T}, \quad (20s)$$

$$\bar{V}_{m,n,t}^{LP} - \bar{V}_{m,n,t-1}^{LP} = \Delta V_{m,n,t}^{LP}, \quad \forall m, n \in \mathbb{P}, t \in \mathbb{T}, \quad (20t)$$

$$\bar{V}_{m,n,t_0}^{LP} = \bar{V}_{m,n,|T|}^{LP}, \quad \forall m, n \in \mathbb{P}, \quad (20u)$$

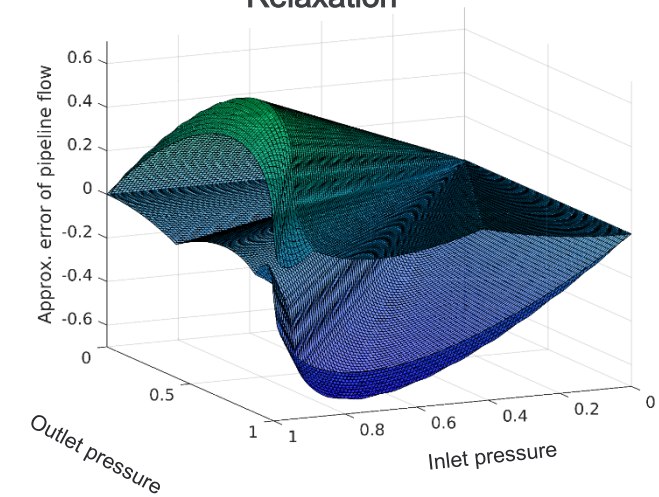
Convex linear relaxation for gas network

Relaxation via McCormick envelopes



Approximation error

Relaxation



Mixed-integer approach

